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Higher Spiritual Abilities (Prolegomena To A Physical Theory)

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Abstract—*Mathematical mechanisms of mind operations are described including concepts, understanding, imagination, thinking, learning, instincts, consciousness, unconscious, intuitions, emotions, including aesthetic emotions. Few basic mathematical principles ("physical laws of mind") are elucidated describing the multiplicity of mind phenomena in correspondence with intuition and psychological and neural data. Predictions and testing of the theory is briefly discussed.*

Keywords: *Mind; Physics; Thinking; Emotions; Aesthetics; Intuition; Learning; Sapience.*

1. INTRODUCTION. ABILITIES OF MIND

The mind understands the world around by relying on "a priori" information, the *models* of the world that were learned previously, an hour ago, earlier in life, in childhood, and ultimately, relying on the inborn genetic information. These internal models of mind are related to Plato's ideas (εἶδε) [^{1,2}], Aristotelian forms [^{3,4}], Kantian ability for understanding [^{5,2}], Jungian archetypes [^{6,2}], and various mechanisms of *concepts* discussed in artificial intelligence, psychology, cognitive science and neural networks [^{7,8}]. Mind brings concept-models in *correspondence* to objects and situations in the world; in the result, there appear *phenomena*, internal mind's perceptions (or representations, which could be conscious or unconscious to varying degrees). Concepts (say, a word "chair", written or spoken) are very different from objects (a chair one sits on). In our brain there are inborn structures that were developed over hundreds of millions of years of evolution specifically to enable fast learning (in childhood) of combining into a single concept-model a spoken, written, drawn, imagined and real chair. Let's note that the "real chair" is what is seen by our eyes, but also what is sensed as a "seat" by the sitting part of our body. Therefore "chair" is a bodily-sensed-spatio-thought concept. The process of comparing concept-models to objects around us is not simple, nor straightforward. An ability for finding correspondence between concepts and objects Kant called *judgment* [⁹]; he identified this ability as a foundation for all higher spiritual abilities of our mind.

An ability for concept-models was evolved during evolution to enhance survivability; it works together with

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other mechanisms developed for this purpose, first of all, instincts and emotions. *Instincts* are like internal sensors that generate signals in neural networks indicating the basic needs of an organism, say hunger [¹⁰]. Connection of instincts and concepts is accomplished by *emotions*. In a usual conversation, «emotions» refer to a special type of behavior: agitation, higher voice pitch, bright eyes, but these are just shows of emotions. Emotions are evaluations «good-bad». Evaluations not according to concepts of good and bad, but direct instinctive evaluations better characterized in terms of pleasure or pain. An emotion evaluates a degree to which a phenomenon (objects or a situation) satisfies our instinctual needs. *Emotions* are signals in neural pathways that carry information about object values from instinct-related brain areas to perceptual, cognitive, decision-making and behavior-generating areas. Emotions «mark» perceived phenomena with their values for instinct satisfaction. There are inborn as well as learned emotional responses. A mathematical description of «marking» of concepts by emotions was first obtained by Grossberg and co-workers in the late 1980s, e.g., [¹¹]. Every instinct generates evaluative emotional signals indicating satisfaction or dissatisfaction of this instinct. Therefore emotions are called evaluative signals. These signals affect the process of comparing concept-models to objects around us (this explains why a hungry person "sees food all around"). So, instinctual needs affect our perception and cognition through emotions; and model-concepts formed in evolution and culture originally are intended for survival and therefore for instinct satisfaction. This *intentionality* of mind was a subject of much discussions and controversies [¹²]. Many emotions originate in ancient parts of the brain, relating us to primates and even to lower animals [¹³]. An ability for concepts includes *learning* and *recognition* (that is creating and remembering models as well as recognizing objects and situations more-or-less corresponding to earlier learned models). A short description in this section did not touch on many of mind's properties, a most important being *behavior* generation. This paper will be mostly concerned just with one type of behavior, *the behavior of learning and recognition*.

The next Section 2 contains a mathematical formulation of the theory (of modeling fields) providing a foundation for an initial description of the mind abilities discussed above and also touches on relationships to psychological and neurophysiological data. Section 3 discusses relationships between the theory and concepts of mind originated in multiple disciplines as well as future directions of experimental programs and theoretical development towards the physical theory of mind.

2. MODELING FIELD THEORY

Neurophysiological data [13] indicates that a hierarchical organization is an important principle of brain organization. This hierarchy is not strict: lateral connections among modules are abundant; and this hierarchy is not one-directional: extensive feedback connections relate "higher" levels back to "lower" levels (e.g., an eye nerve connecting retina to visual cortex has more feedback connections, from the cortex to the retina, than feedforward ones, from the retina to the cortex). Existence of feedback connections was appreciated for a while, and this gave rise to an idea of combining "top-down" processing with the "bottom-up" one. Yet, the mathematical nature of the mechanisms of these connections was subject of many controversies [2]. This section describes a basic mechanism of interaction between two adjacent hierarchical levels of signals (fields of neural activation); sometimes, it will be more convenient to talk about these two signal-levels as an input to and output from a (single) processing-level. At each level, the output are concepts recognized (or formed) from input signals. At the bottom of the mind hierarchy, the input is sensory signals, the activation levels of sensory cells, and the output are "concepts" formed or recognized at this level; this output neuronal field of activated "concepts" serves as input to the next level; higher up the hierarchy, the inputs are objects or situations recognized at lower levels and outputs are more complex, more general situation-concepts or relationship-concepts.

Internal Models, Learning, And Similarity

During the learning process, new associations of input signals are formed resulting in the evolution of new concepts. Input signals $\{X(n)\}$, is a field of input neuronal synapse activation levels, n enumerates the input neurons and $X(n)$ are the activation levels; a set of concept-models $\{h\}$ is characterized by the models (representations) $\{M_h(n)\}$ of the signals $X(n)$; each model depends on its parameters $\{S_h\}$. In a highly simplified description of a visual cortex, n enumerates the visual cortex neurons, $X(n)$ are the "bottom-up" activation levels of these neurons coming from the retina through visual nerve, and $M_h(n)$ are the "top-down" activation levels (or priming) of the visual cortex neurons from previously learned object-models¹⁴. The learning process attempts to "match" these top-down and bottom-up activations by selecting "best" models and their parameters. Mathematically, learning increases a similarity measure between the sets of models and signals, $L(\{X(n)\}, \{M_h(n)\})$. The similarity measure is a function of model parameters and associations between the input synapses and concepts-models. It is constructed in such a way that any of a large number of objects can be recognized, no matter if they appear on the left or on the right. Correspondingly, a similarity measure is designed so that it treats each concept-model as an alternative for each subset of signals

$$L(\{X\}, \{M\}) = \prod_{n \in N} \sum_{h \in H} r(h) l(X(n) | M_h(n)); \quad (1)$$

here $l(X(n) | M_h(n))$ (or simply $l(n|h)$) is a conditional partial similarity between one signal $X(n)$ and one model $M_h(n)$, and all possible combinations of signals and models are accounted for in this expression. Parameters $r(h)$ are proportional to the number of signals $\{n\}$ associated with the model h .

In the process of learning, concept-models are constantly modified. From time to time a system forms a new concept, while retaining an old one as well; alternatively, old concepts are sometimes merged. Formation of new concepts and merging of old ones require a modification of the similarity measure (1); the reason is that more models always result in a better fit between the models and data. This is a well known problem, it can be addressed by reducing (1) using a "penalty function", $p(N, M)$ that grows with the number of models M , and this growth is steeper for a smaller amount of data N . For example, an asymptotically unbiased maximum likelihood estimation leads to multiplicative $p(N, M) = \exp(-N_{par}/2)$, where N_{par} is a total number of adaptive parameters in all models (this penalty function is known as Akaike Information Criterion, see [2] for further discussion and references).

Fuzzy Dynamic Logic And MFT

The learning process consists in estimating model parameters S_h and associating subsets of signals with concepts by maximizing the similarity (1). Note, that (1) contains a large number of combinations of models and signals, a total of H^N items; this was a cause for the combinatorial complexity of the past algorithms discussed in detail later. Modeling field theory (MFT) solves this problem by utilizing fuzzy dynamic logic [2,15]. MFT introduces association variables $f(h|n)$

$$f(h|n) = r(h) l(n|h) / \sum_{h' \in H} r(h') l(n|h'). \quad (2)$$

These variables give a measure of correspondence between a signal $X(n)$ and a model M_h relative to all other models, h' . A mechanism, an internal dynamics, of the Modeling Fields (MF) is defined as follows,

$$\begin{aligned} df(h|n)/dt &= f(h|n) \sum_{h' \in H} \{[\delta_{hh'} - f(h'|n)] \cdot [\partial \ln l(n|h') / \partial M_{h'}]\} \\ \partial M_{h'} / \partial S_{h'} \cdot dS_{h'} / dt, \end{aligned} \quad (3)$$

$$dS_h / dt = \left\{ \sum_N f(h|n) [\partial \ln l(n|h) / \partial M_h] \partial M_h' / \partial S_h \right\}, \quad (4)$$

here $\delta_{hh'}$ is 1 if $h=h'$, 0 otherwise. Parameter t is the time of the internal dynamics of the MF system (like a number of internal iterations). The following theorem was proven.

Theorem. Equations (2) through (4) define a convergent dynamic system MF with stationary states defined by $\max\{S_n\}L$.

In plain language this means that the above equations indeed result in concept-models in the "mind" of the MFT system, which are most similar [in terms of similarity (1)] to the sensory data. Despite a combinatorially large number of items in (1), a computational complexity of the MF method is relatively low, it is linear in N , it could be implemented by a physical system (like the brain) and therefore it may correspond to the working of the mind. These equations describe a 'semantic closure' sustaining its operations; when input signals continuously coming in real time the above equations should be supplemented by a mechanism retaining input signals in working memory for a finite period of time.

Dynamic logic and combinatorial complexity

Combinatorial complexity of the past algorithms, as indicated in the previous section, is related to a basic structure of a similarity measure (1). It has also been related to the type of logic, underlying various algorithms and neural networks [16]. Formal logic is based on the "law of excluded third", according to which every statement is either true or false and nothing in between. Therefore, algorithms based on formal logic have to evaluate every little variation in data or internal representations as a separate logical statement; a large number of combinations of these variations causes combinatorial complexity. In fact, combinatorial complexity of algorithms based on logic has been related to the Gödel theory: it is a manifestation of the incompleteness of logic in finite systems [17]. Multivalued logic and fuzzy logic were proposed to overcome limitations related to the law of excluded third [18]. Yet the mathematics of multivalued logic is no different in principle from formal logic. Fuzzy logic encountered a difficulty related to the degree of fuzziness: if too much fuzziness is specified, the solution does not achieve a needed accuracy, if too little, it might become similar to formal logic, and adapting the required degree of fuzziness by 'brute force' at every processing step for every combination of models and data would lead to combinatorial complexity. To summarize the above discussion, formal logic starts with exact knowledge (or assumptions) and results in exact deductions, but if exact knowledge is unavailable, trying all kind of assumptions leads to combinatorial complexity. Fuzzy logic starts with fuzzy knowledge (or assumptions) and leads to fuzzy deductions, which may not satisfy the required accuracy. Dynamic logic starts with fuzzy knowledge-assumptions and proceed to exact deductions – much like human mind does.

MFT Hierarchical Organization

The previous sub-section described a single processing layer in a hierarchical MFT system. An input to each layer is a set of signals $X(n)$, or in neural

terminology, an input field of neuronal activations. An output are the activated models $M_n(S_n, n)$; it is a set of models or concepts recognized in the input signals. Equations (2-4) describe a loop-process: at each iteration (or internal-time t) the l.h.s. of the equations contain association variables $f(hln)$ and other model parameters computed at the previous iteration. In other words, the output models "act" upon the input to produce a "refined" output models (at the next iteration). This process is directed at increasing the similarity between the models and signals. It can be described as an internal behavior generated by the models.

The model output initiate other actions as well. First, activated models (neuronal axons) serve as input signals to the next processing layer, where more general concept-models are recognized or created. Second, concept-models along with the corresponding instinctual signals and emotions may activate behavioral models and generate behavior directed into the outside world (a process not contained within the above equations). In general, a higher level in a hierarchical system provides a feedback input into a lower level. For example, sensitivity of retinal ganglion cells depends on the objects and situations recognized higher up in the visual cortex; or a gaze is directed based on which objects are recognized in the field of view. Concept-objects identified at the output of the lower level of MFT system become input signals to the next MFT level which identifies more general concepts of relationships among objects and situations; at the same time more general concepts of understanding identified at a higher level activate behavioral concept-models that affect processes at a lower level. The agent processes, or the loop-processes of model-concept adaptation, understanding and behavior generation continue up and down the hierarchy of the MFT levels.

The MFT operations involves adaptation of multiple models or concepts; these model-adaptation processes are 'agents', to some extent they are independent, yet some model-concept-agents interact when they are associated with the same data pieces. MFT therefore is an intelligent system composed of multiple adaptive intelligent agents, which possess a degree of autonomy yet interact among themselves. Each concept-model-agent along with the similarity measure and behavioral response is a continuous loop of operations, interacting with other agents from time to time; an agent is "dormant" until activated by a high similarity value. When activated, it is adapted to the signals and other agents, so that the similarity increases. Every piece of signal may activate several concepts, or agents, in this way input signals provide evidence for the presence of various objects (or concepts). Agents compete with each other for evidence (data), while adapting to the new signals.

3. MFT THEORY OF MIND

MFT Dynamics

Equations (2-4) describe an elementary process of perception or cognition, in which a large number of model-concepts compete for incoming signals, model-concepts are modified and new ones are formed, and eventually, more or less definite

connections [high or low values of $f(h|n)$, varying between 0 and 1] are established among signal subsets on the one hand, and model-concepts on the other. Perception refers to processes in which the input signals come from sensory organs and model-concepts correspond to objects in the surrounding world. Cognition refers to higher levels in the hierarchy where the input signals are concepts activated at lower levels and model-concepts are more complex and correspond to situations and relationships among lower-level concepts.

A salient mathematical property of this processes ensuring a smooth convergence is a correspondence between uncertainty in models (that is, in the knowledge of model parameters) and uncertainty in associations $f(h|n)$. In perception, as long as model parameters do not correspond to actual objects, there is no match between models and signals; many models poorly match many objects, and associations remain fuzzy (nor 1 nor 0). Eventually, one model (h') wins a competition for a subset $\{n'\}$ of input signals $X(n)$, when parameter values match object properties, and $f(h'|n')$ values become close to 1 for $n \in \{n'\}$ and 0 for $n \notin \{n'\}$. This means that this subset of data is recognized as a specific object (concept). Upon the convergence, the entire set of input signals $\{n\}$ is divided into subsets, each associated with one model-object, uncertainties become small, and fuzzy a priori concepts become crisp concepts. Cognition is different from perception in that models are more general, more abstract, and input signals are the activation signals from concepts identified (cognized) at a lower hierarchical level; the general mathematical laws of cognition and perception are similar in MFT and constitute a basic principle of the mind organization. Let us discuss relationships between the MFT theory and concepts of mind developed in psychology, philosophy, linguistics, aesthetics, neurophysiology, neural networks, artificial intelligence, pattern recognition, and intelligent systems.

Elementary Thought-Process, Conscious and Unconscious

A thought-process or thinking involves a number of sub-processes and attributes, including internal representations and their manipulation, attention, memory, concept formation, knowledge, generalization, recognition, understanding, meaning, prediction, imagination, intuition, emotion, decisions, reasoning, goals, behavior, conscious and unconscious [27, 2]. A "minimal" subset of these processes involves mechanisms for afferent and efferent signals, Grossberg, S. (1988), in other words, bottom-up and top-down signals coming from outside (external sensor signals) and from inside (internal representation signals). According to Carpenter and Grossberg [19] every recognition and concept formation process involves a "resonance" between these two types of signals. In MFT, at every level in a hierarchy the afferent signals are represented by the input signal field X , and the efferent signals are represented by the modeling field signals M_h ; resonances correspond to high similarity

measures $l(n|h)$ for some subsets of $\{n\}$ that are "recognized" as concepts (or objects) h . The mechanism leading to the resonances is given by (2-4), and we call it an elementary thought-process. The elementary thought-process involves elements of conscious and unconscious processes, imagination, memory, internal representations, concepts, instincts, emotions, understanding and behavior as further described later.

A description of working of the mind as given by the MFT dynamics was first provided by Aristotle [20], describing thinking as a learning process in which an a priori form-as-potentiality (fuzzy model) meets matter (sensory signals) and becomes a form-as-actuality (a concept). Jung suggested that conscious concepts are developed by mind based on genetically inherited structures of mind, archetypes, which are inaccessible to consciousness [21] and Grossberg suggested that only signals and models attaining a resonant state (that is signals matching models) reach consciousness [27].

Understanding

In the elementary thought process, subsets in the incoming signals are associated with recognized model-objects, creating *phenomena* (of the MFT-mind) which are *understood* as objects, in other words *signal subsets* acquire *meaning* (e.g., a subset of retinal signals acquires a meaning of a chair). There are several aspects to understanding and meaning. First, object-models are connected by emotional signals [11, 22, 2] to instincts that they might satisfy, and also to behavioral models that can make use of them for instinct satisfaction. Second, an object is understood in the context of a more general situation in the next layer consisting of more general concept-models, which accepts as input-signals the results of object recognition. That is, each recognized object-model (phenomenon) sends (in neural terminology, activates) an output signal; and a set of these signals comprises input signals for the next layer models, which 'cognize' more general concept-models. And this process continues up and up the hierarchy of models and mind toward the most general models a system could come up with, such as models of universe (scientific theories), models of self (psychological concepts), models of the meaning of existence (philosophical concepts), models of a priori transcendent intelligent subjects (theological concepts).

Imagination

Imagination involves excitation of a neural pattern in a visual cortex in the absence of an actual sensory stimulation (say, with closed eyes) [27]. Imagination was often considered to be a part of thinking processes; Kant [23] emphasized the role of imagination in the thought process, he called thinking "a play of cognitive functions of imagination and understanding". Whereas the pattern recognition and artificial intelligence algorithms of the recent past would not know how to relate to this [24], the Carpenter and Grossberg resonance model [19] and the MFT dynamics both describe imagination as an inseparable part of thinking: imagined patterns are top-down signals that *prime* the perceiving cortex areas (*priming* is a neural terminology for making neural cells to be more readily excited). In MFT, the imagined neural patterns are given by

models M_h . MFT (in agreement with neural data) just adds details to Kantian description: thinking is a play of *higher-hierarchical-level* imagination and *lower-level* understanding. Kant identified this “play” [described by (3-6) or (7-12)] as a source of aesthetic emotion; modeling aesthetic emotion in MFT is described later.

Mind vs. Brain

Historically, the mind is described in psychological and philosophical terms, whereas the brain is described in terms of neurobiology and medicine. Within scientific exploration the mind and brain are different description levels of the same system. Establishing relationships between these descriptions is of great scientific interest. Today we approach solutions to this challenge [25], which eluded Newton in his attempt to establish physics of “spiritual substance” [26]. General neural mechanisms of the elementary thought process (which are similar in MFT and ART have been confirmed by neural and psychological experiments, this includes neural mechanisms for bottom-up (sensory) signals, top-down “imagination” model-signals, and the resonant matching between the two [27]. Adaptive modeling abilities are well studied with adaptive parameters identified with synaptic connections [28]; instinctual learning mechanisms have been studied in psychology and linguistics [29].

Instincts and Emotions

Functioning of the mind and brain cannot be understood in isolation from the system’s “bodily needs”. For example, a biological system (and any autonomous system) needs to replenish its energy resources (eat); this and other fundamental unconditional needs are indicated to the system by instincts, which could be described as internal sensors. Emotional signals, generated by this instinct are perceived by consciousness as “hunger”, and they activate behavioral models related to food searching and eating. In this paper we are concerned primarily with the behavior of recognition: instinctual influence on recognition modify the object-perception process (3) - (6) in such a way, that desired objects “get” enhanced recognition. It can be accomplished by modifying priors, $r(h)$, according to the degree to which an object of type h can satisfy a particular instinct. Details of these mechanisms are not considered here, except for a specific instinct considered below.

Aesthetic Emotions and Instinct for Knowledge

Recognizing objects in the environment and understanding their meaning is so important for human evolutionary success that there has evolved an instinct for learning and improving concept-models. This instinct (for knowledge and learning) is described in MFT by maximization of similarity between the models and the world, (1). Emotions related to satisfaction-dissatisfaction of this instinct are perceived by us as harmony-disharmony (between our understanding of how things

ought to be and how they actually are in the surrounding world). According to Kant (1790) [9] these are aesthetic emotions (emotions that are not related directly to satisfaction or dissatisfaction of bodily needs).

Beauty. Harmony is an elementary aesthetic emotion related to improvement of object-models. Higher aesthetic emotions are related to the development of more complex “higher” models: we perceive an object or situation as aesthetically pleasing if it satisfies our learning instinct, that is the need for improving the models and increasing similarity (1). The highest forms of aesthetic emotions are related to the most general and most important models. According to Kantian analysis [Error! Bookmark not defined.], among the highest models are models of the meaning of our existence, purposiveness or intentionality, and beauty is related to improving these models: we perceive an object or a situation as beautiful, when it stimulates improvement of these highest models of meaning. Beautiful is what “reminds” us of our purposiveness. The mathematical description of the emotion of beautiful is given by increase of similarity measure related to the most general models of our purpose.

Intuition

Intuition includes an intuitive perception (imagination) of object-models and their relationships with objects in the world, as well as higher-level models of relationships among simpler models. Intuition involves fuzzy unconscious concept-models, which are in a state of being learned and being adapted toward crisp and conscious models (a theory); such models may satisfy or dissatisfy the knowledge instinct in varying degrees before they are accessible to consciousness, hence the complex emotional feel of an intuition. The beauty of a physical theory discussed often by physicists is related to satisfying our feeling of purpose in the world, that is, satisfying our need to improve the models of the meaning in our understanding of the universe.

Theory Testing and Future Directions

The general neural mechanisms of the elementary thought process, which includes neural mechanisms for bottom-up (sensory) signals, top-down “imagination” model-signals, and the resonant matching between the two [27], have been confirmed by neural and psychological experiments (these mechanisms are similar in MFT and ART [19]. Adaptive modeling abilities are well studied and adaptive parameters have been identified with synaptic connections [28]; instinctual learning mechanisms have been studied in psychology and linguistics [30]. Ongoing and future research will confirm, disprove, or suggest modifications to specific mechanisms of model parameterization and parameter adaptation (4), reduction of fuzziness during learning (2), similarity measure (1) as a foundation of aesthetic instinct for knowledge, relationships between psychological and neural mechanisms of learning on the one hand and, on the other, aesthetic feelings of harmony and emotion of beautiful. Differentiated forms of (1) need to be developed for various forms of the knowledge instinct (child development, language learning, emotional

intelligence, etc.) Future experimental research needs to study in details the nature of hierarchical interactions: to what extent the hierarchy is "hardwired" vs. adaptively emerging; what is a hierarchy of learning instinct? A theory and experimental data will have to be developed for differentiated form of knowledge instinct and differentiated aesthetic emotions and their role in learning and intelligence.

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